

# Tension and Spring force

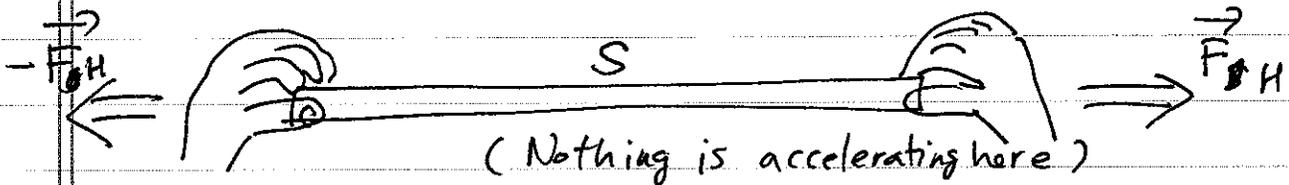
(Restoring forces)



If your body is pulled like this  
what is your reaction?!

To restore!

String, rope, spring act the same way.



Your hand is stretching the object  $S$   
with force  $\vec{F}_{H}$ , how does that  
object react? It does this:



At contacts, the object  $S$  applies

$\vec{F}_S$  and  $-\vec{F}_S$

$\Rightarrow \vec{F}_S = -\vec{F}_H$  by Newton's 3<sup>rd</sup> law

The forces  $\vec{F}_S$  and  $-\vec{F}_S$  tend to  
restore the shape of  $S$

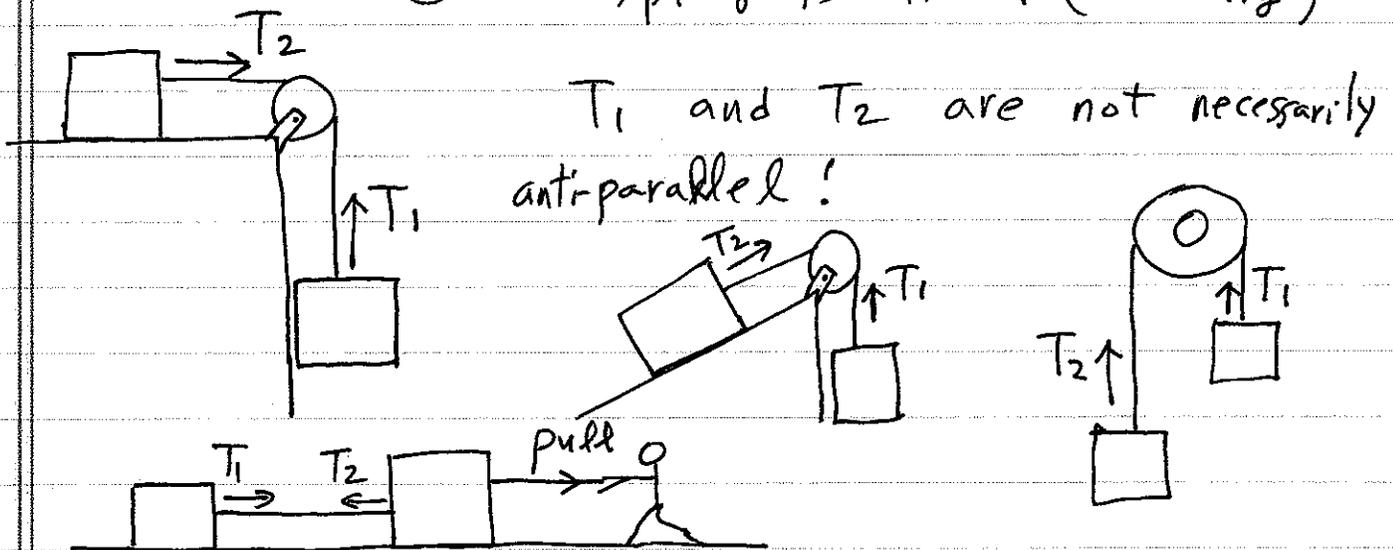
resist the change of  $S$

$\Rightarrow$  "restoring force" !

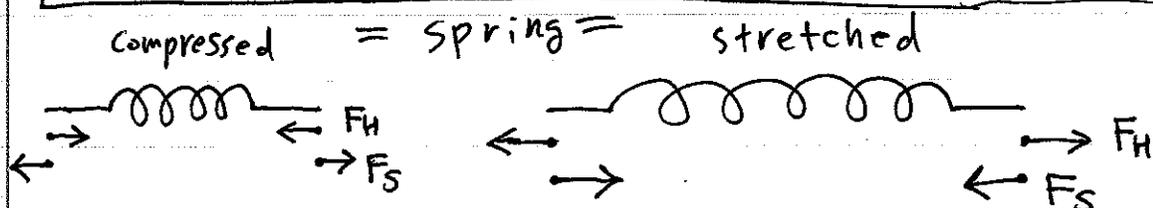
- ① String, rope ... :  $\vec{F}_S$  is called  $(-\vec{F}_S)$  "Tension"
- ② Spring ... :  $\vec{F}_S$  is called Spring force

Both "delivers" force.

- Differences :
- ① ... can be only stretched.
  - ② ... can be stretched and compressed.
  - ① ... string, rope can be in any curve (using pulley)
  - ② ... Spring is linear (normally)



However,  $T_1 = T_2$  (magnitude the same)  
 Always True if the string, rope is not accelerating.  
 True even when accelerating, if mass of (string) is negligible.

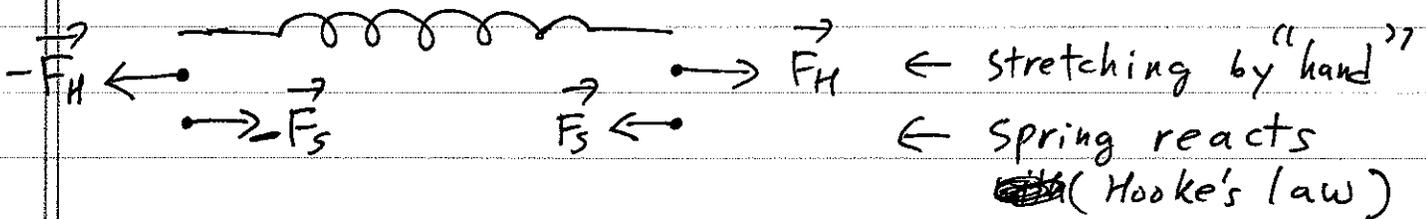


# Hooke's law

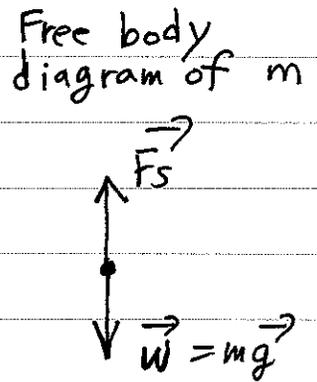
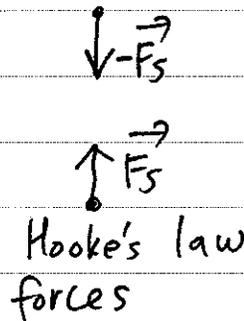
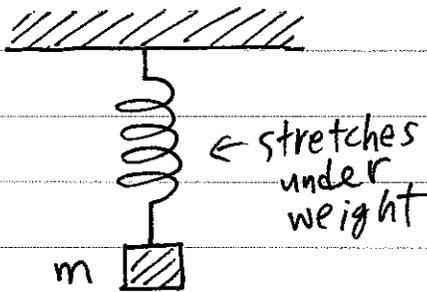
$$F_s = -kx$$

$\uparrow$  means "restoring force" oppose the change  $x$   
 $\uparrow$  spring constant  
 $\left[ \begin{array}{l} \text{the length of spring} \\ - \text{ the normal length of spring} \end{array} \right]$   
 $\uparrow$  no compression no stretching

**Important**  $x$  here is not a coordinate!  
 $F_s$  is (opposite in direction) ~~at the~~ at the two ends of spring (equal in magnitude)



What is spring good for?  
 Measure force! weight!

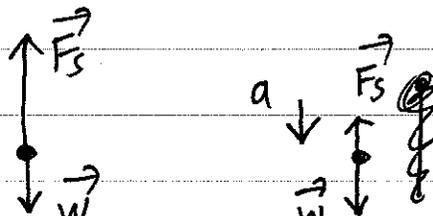


**Note** The same ~~comment~~ comment as ~~in~~ in the previous page applies for the two spring forces at the two ends of a spring

$kx = F_s = W$   
 measure  $x \Rightarrow$  know  $W$ !

Elevator revisited  $a \uparrow$

True weight  $\vec{W}$  never changes.  
 The apparent weight  $\vec{F}_s$  changes!!



What if  $a \downarrow, a \geq g$ ?

cf. Ex 4.9